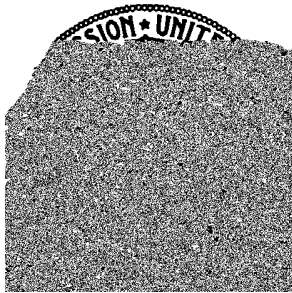


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Competition, Contracts, and Innovation

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Competition, Contracts, and Innovation

Christopher J. Metcalf and John D. Simpson¹

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Abstract

Our paper contributes to the literature on the relationship between innovation and market power by considering how changes in the intensity of product market competition affect innovation when managerial compensation is a linear function of firm profits. Changes in the intensity of product market competition affect both the return from innovation and the cost of inducing managers to innovate. Several recent papers account for both the returns-to-investment effect and the agency-cost effect in analyzing the effect of additional product market competition on incentives to innovate (see e.g., Schmidt (1997), Raith (2003), and Piccolo, D'Amato, and Martina (2008)). Our model differs from these papers in the type of contract that we assume firms can use to induce innovation. With linear profit-sharing contracts, the cost of a non-drastic innovation declines as product market competition increases because the increment gained from innovation becomes a larger fraction of the total profit. We argue that this decline in the cost of attaining innovation as competition increases means that competition will often lead to more innovation even in models where the returns to innovation otherwise would fall as competition increases.

1 Introduction and Literature Review

Does market power facilitate innovation? If so, under what circumstances should competition policy tolerate the short-term allocative inefficiency associated with market power in order to obtain higher levels of innovation? These two questions have been a

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central issue in Industrial Organization for 50 years. While simple answers have proved elusive, numerous papers have made significant progress toward addressing these questions. Our paper seeks to add to this stock of knowledge by considering how product market competition affects innovation when managerial compensation is a linear function of firm profits.

Changes in the intensity of product market competition affect both the return from innovation and the cost of inducing managers to innovate. An extensive literature examines the effect of product market competition on the return from innovation and finds that greater product market competition can lead to either increased innovation or decreased innovation depending on the assumptions made about factors such as the nature of competition before and after the innovation, whether the innovation can be readily copied, and whether rivals can also innovate. (see e.g., Arrow (1962); Tirole (1988); Schumpeter (1947); Qiu (1997); Vives (2008)). Another set of papers examines the effect of product market competition on the cost of inducing managerial effort and finds that increased competition, measured as the number of entrepreneurial firms (i.e., without agency problems), either reduces agency problems or increases agency problems depending on the agent's utility function (e.g., Oliver Hart (1983) and Scharfstein (1988)). Finally, several recent papers account for both the returns-to-investment effect and agency-cost effect in analyzing the effect of additional product market competition on incentives to innovate (see e.g., Schmidt (1997), Raith (2003), and Piccolo, D'Amato, and Martina (2008)).

2 Model

We consider a three stage model: In stage one, each of two symmetric ...rms simul-

Specifically, we assume that each firm with competitor m

$$d v | p \mathbb{E} f \gg \{ > f \frac{E^2 f^2}{E e f^2 E \cdot f^2} \{ 2 f^2 n 2 E \cdot f 2 f f^2$$

Let us ...rst focus only on the case where it is the unique pure strategy equilibrium

Figure 1: Baseline Example: $d v | p$ and $v | p$ for

$$E > f > \{ \bullet \}_{e > \frac{2}{f}}$$

As an aside, let us now briefly consider the parameter region where it is a pure strategy equilibrium for only one owner to invest. Proposition 1 shows that an owner's additional profit from having a lower marginal cost first decreases and then increases as competition (f) increases. Combining this result with the result for the case where both owners invest, and recalling that $d v | p \geq v | p$, shows that the form of the equilibrium can change in a number of ways as f increases. Specifically, depending on the level of j (the cost of innovating), the relationship between competition and investment may result in the following: (1) no innovation for any level of competition ($j \geq d v | p - E f$), (2) no innovation followed by innovation by only one firm ($d v | p - E f > j > d v | p - E f$), (3) innovation by both firms, followed by innovation by one firm, followed by no innovation, followed by innovation by only one firm ($4 > d v | p > j > d v | p - E f$), (4) innovation by both firms followed by innovation by only one firm ($v | p - E f > j > 4 > d v | p$), (5) innovation by both firms for all levels of competition ($j < v | p - E f$). Note that if innovation is costless, $j = 0$, then

it is the dominant strategy for both firms to invest.

These results arise in large part because of the lumpiness of innovation investment. This lumpiness gives rise to asymmetric outcomes in a symmetric situation, and this asymmetry in turn leads to the increase in investment after the initial decrease. If investment was not lumpy, then as the return to investment falls with increased competition (given that the opponent is also investing) both firms would reduce investment leading potentially to a symmetric equilibrium. Since investment is lumpy, as the re-

$$e_{v|p} \geq A_j \quad (7)$$

Since $e_{v|p} \geq A_j$, equation 7 is the binding condition in terms of defining the region of f such that innovating is a dominant strategy for managers of both firms. Define f_j^* as the implicit function defined by: $e_{v|p} = A_j$. Define f_j^* such that for all f that $f > f_j^*$, the equilibrium of the stage 2 has both managers investing as a dominant strategy. Since the manager receives only a share of the additional profit from innovating, an immediate result is that for any e , fewer situations induce both firms to invest than in the model without an agency problem:

Proposition 2 For any $e \in E$, $f_j^* > f_j^*$.

Proof. From proposition 1, $e_{v|p} \geq A_j$, $\frac{C_{v|p}}{C_f} > f$, and $f > e$. $\frac{C_{v|p}}{C_f} > f$ implies that this implicit function is well-defined. If f is such that $e_{v|p} < j$, it must be that $e_{v|p} < A_j$. ■

A second result is that an owner must pay a manager a larger share of firm profit in order to obtain innovation as competition increases. However, because the firms' overall profit decreases as competition increases, the total amount paid to managers decreases as competition increases. Denote $e_{v|p}^j$ as the minimum e that will induce the agent to innovate given j and the other firm investing, i.e., $e_{v|p}^j = \frac{j}{v|p}$.⁹

Proposition 3 For the case where both rivals invest, when $j > e_{v|p}$, the fraction of profits needed to induce the manager to invest increases as competition increases,

Proof. See Appendix. ■

Denote $e_{d|p}$ as the minimum e that will induce the agent to innovate given j and the other ...rm not investing, i.e., $e_{d|p} = \frac{j}{d|p}$.¹⁰ Since $e_{d|p} > e_{v|p}$, it is the case that $e_{v|p} > e_{d|p}$.

Since the principal will not pay an excess sum to induce an action, the only pure strategy equilibria of stage 1 are $E_{v|p} > e_{v|p}$, $E_{d|p} > e_{d|p}$, $E_{v|p} > e_{d|p}$, and $E_{d|p} > e_{v|p}$ (See Table 2.) In stage 2, the choices of e from the stage 1 determine the equilibrium investments. If the principals choose $E_{v|p} > e_{v|p}$ then investing is a dominant strategy for both agents, and thus $E_{v|p} > e_{v|p}$ is the unique stage 2 Nash Equilibrium. If the principals choose $E_{v|p} > e_{d|p}$ then investing remains the dominant strategy for the agent of ...rm 1. However, since the agent for ...rm 2 will only invest when the agent for ...rm 1 declines to invest, the unique stage 2 Nash Equilibrium is now $E_{d|p} > e_{d|p}$. Therefore, an equilibrium is not formed by $E_{v|p} > e_{d|p}$ because principal 2 would unilaterally deviate to $E_{d|p} > e_{d|p}$ since $E_{d|p} > e_{d|p} > E_{v|p} > e_{d|p}$ similarly for $E_{d|p} > e_{v|p}$. If the principals choose $E_{d|p} > e_{v|p}$ then investing is a dominant strategy for the agent of ...rm 1 while not investing is a dominant strategy for the agent of ...rm 2. Thus, the unique stage 2 Nash Equilibrium is $E_{d|p} > e_{d|p}$. However, an equilibrium is not formed by $E_{d|p} > e_{v|p}$ because principal 1 would unilaterally deviate to $E_{v|p} > e_{v|p}$ since $E_{v|p} > e_{v|p} > E_{d|p} > e_{v|p}$ similarly for $E_{v|p} > e_{d|p}$. If the principals choose $E_{v|p} > e_{d|p}$ then, there are two pure strategy Nash equilibria: $E_{v|p} > e_{v|p}$ and $E_{d|p} > e_{d|p}$. Therefore, an equilibrium is not formed by $E_{v|p} > e_{d|p}$ (with a pure strategy equilibrium in stage 2) because the principal whose agent does not invest in stage 2 would unilaterally deviate from $e_{d|p}$ to 0 since $E_{d|p} > e_{d|p} > E_{v|p} > e_{d|p}$. If the principals choose $E_{d|p} > e_{v|p}$ then for both agents not investing is a dominant strategy, thus the unique Nash equilibrium is $E_{d|p} > e_{d|p}$. Neither $e_{v|p}$ nor $e_{d|p}$ is ever a dominant strategy in stage 1 because in response to

¹⁰ $e_{d|p} = \frac{j + f^5 + f^5}{(5 + f^5) + (5 + f^5) + (5 + f^5) + (5 + f^5) + (5 + f^5)}$

and $e_{v|p}$

competition leads to greater innovation is most extensive where cost is relatively low and where innovation leads to relatively small cost reductions.

Proposition 4 There is $j_{v|p} \in (f, 1)$ such that if $j > j_{v|p}$ then the unique (pure strategy) equilibrium is for both principals to induce the agents to invest by setting $e = e_{v|p}$ and if $j < j_{v|p}$ then both principals inducing investment is not an equilibrium.

There is an α and a $f \in (0, 1)$ such that if $\alpha > \alpha$ and $f > f$, then there are $f_0 \in (0, 1)$ and $f_X \in (0, 1)$ such that $\frac{C_{j|p}}{C_f} > \alpha$ if $f_0 > f > f_X$ otherwise $\frac{C_{j|p}}{C_f} < \alpha$.¹² Finally, $\frac{C_b}{C} > f$, $\frac{C_b}{C} > \alpha$, $\frac{C_b}{C} > \alpha$, $\frac{C_b}{C} > f$, and $\frac{C_b}{C} > f$.

Proof. See Appendix. ■

¹²For instance at $f = \frac{4}{5}$, then $\frac{C_{j|p}}{C_f} > \alpha$ if $\alpha > \frac{4}{5}$ and $f > \frac{6}{4}$.

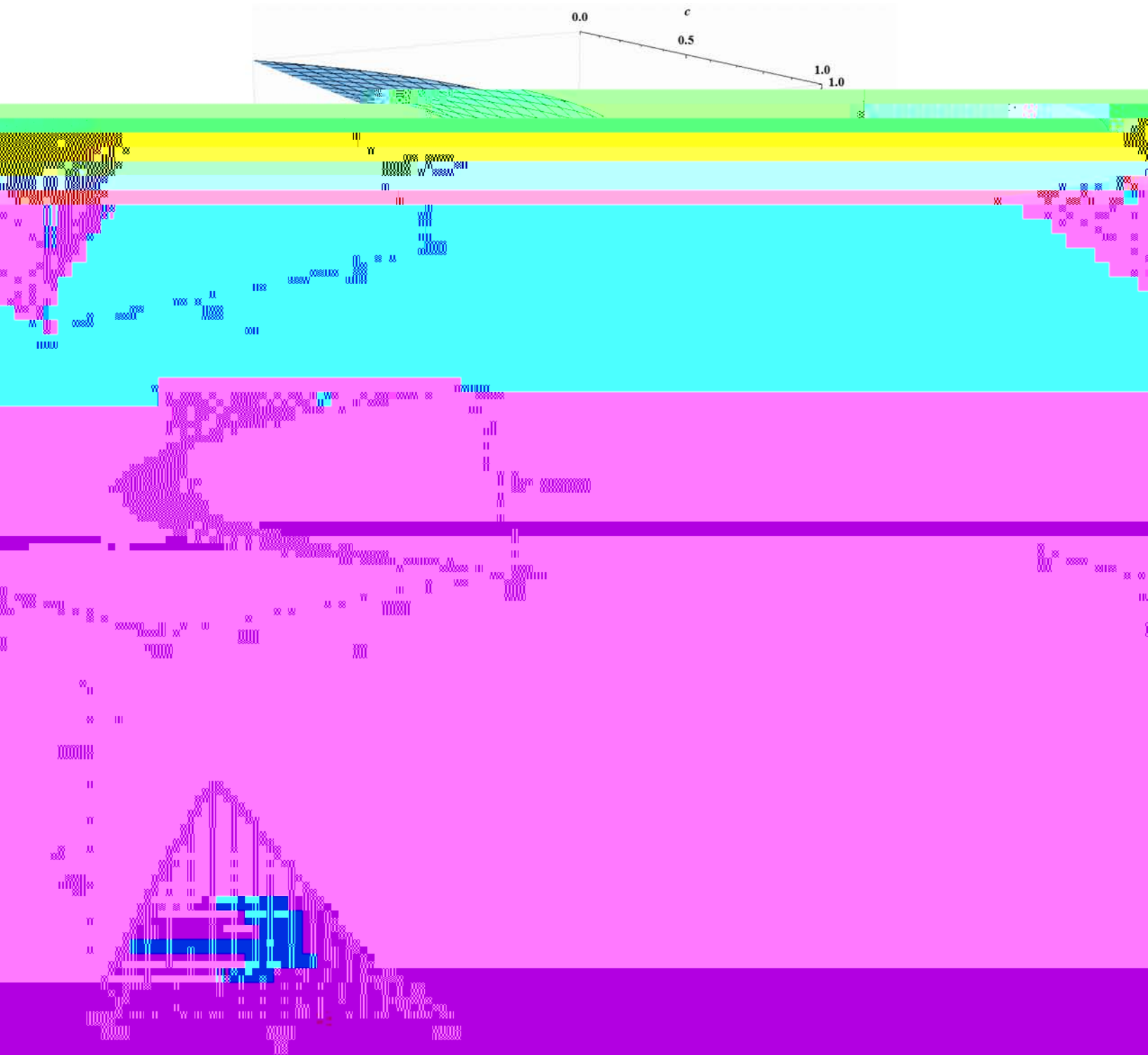


Figure 2: The Investment Increases with Competition Intensity Region:
 For each $\beta > \beta^*$ the upper bound and lower bound are shown for the region of β for which
 as f increases, the extent of the investment region increases.

The results from proposition 4 can also be visualized through two examples in which $j_{v|p}$ declines slightly over a narrow range when competition is low, increases significantly over a broad range as competition intensifies, and eventually declines sharply as competition further intensifies. In example 1, $\frac{c}{f} > \frac{c}{f_2} > \frac{c}{f_1}$ thus an innovation would reduce marginal cost by 50 percent. In this example, the highest level of cost for which a firm with an agent would invest when its rival also invests ($j_{v|p}$) initially falls almost imperceptibly, then rises over almost the entire range of the substitution parameter f , then falls sharply as competition becomes very intense. In example 2, $\frac{c}{f} > \frac{c}{f_2} > \frac{c}{f_1}$ thus, an innovation would reduce marginal cost by 40 percent. In this example, $j_{v|p}$ declines modestly when the substitution parameter is low, increases substantially when the substitution parameter has moderate values, and then

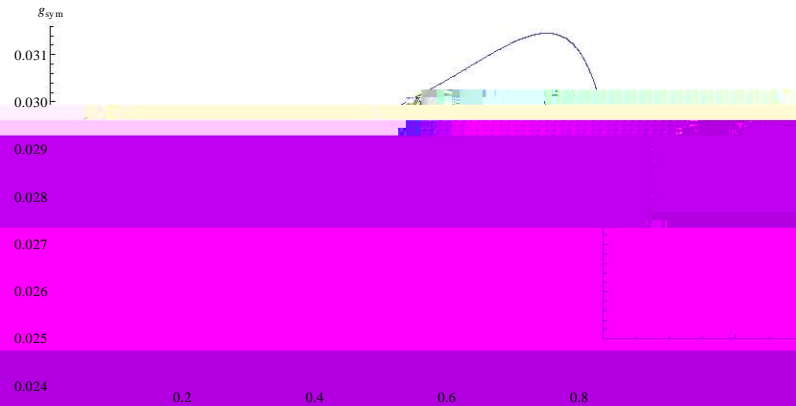


Figure 4: Example 2: $E > f > \frac{1}{2} > \frac{1}{D}$

In our model, the relationship between product market competition and innovation changes dramatically when we add the assumption that firms can only use profit-sharing contracts to motivate managers to innovate: Absent agency problems, the level of innovation declines monotonically with greater product market competition; when firms must use profit-sharing contracts to solve agency problems, the level of innovation initially declines slightly, then rises over a broad region, and then falls sharply.

The intuition for this result can be seen by combining the equality formed by condition 8 and e

incremental profit to the total profit because the owner will pay a fraction of the total but the size of the fraction depends on the size of the increment relative to j .¹³

The change of the boundary of the investment region, $\frac{C_{j|p}}{C_f}$, can then be written as in equation 12 (since $\frac{C_{v|p}}{C_f} > f$ and $\frac{C_u}{C_f} < f$ from Proposition 3).¹⁴

$$\frac{C_{j|p}}{C_f} = \frac{C_{v|p}}{C_f} \cup \frac{C_u}{C_f} \quad (12)$$

The maximum cost where both firms innovate decreases with competition if and only if $\frac{C_{v|p}}{C_f} \cup$ is greater than $\frac{C_u}{C_f} \quad v|p$. In other words, if the effect of the decrease in the incremental profit is greater than the effect of the decrease in the cost of investing multiplier (relative to the levels) then investment decreases with competition. This can be understood as the decrease in the return to innovation dominating the decrease in the cost of inducing innovation. The maximum cost where both invest increases with competition if $\frac{C_u}{C_f} \quad v|p > \frac{C_{v|p}}{C_f} \cup$. This can be understood as the decrease in the cost of inducing innovation dominating the decrease in the return to innovation. Therefore, the non-monotonic relationship between product market competition and innovation results from one effect being dominant over the other for some ranges of competitive intensity but not all.

¹³Formally, the cost can be divided into two parts, a fraction of the incremental profit and a fraction of the baseline profit. The fraction of the incremental profit must equal j to induce innovation, which determines $e_{v|p}$. This same fraction of the baseline profit also becomes part of the cost. Therefore for a given level of incremental profit, if the baseline profit decreases then the cost decreases because the necessary fraction stayed the same but the total payment decreased. Alternatively, for a given level of total profit, as more of the profit is shifted into the increment from the baseline, the necessary fraction of the total decreases since j stayed the same but $v|p$ increased and therefore the cost decreases (because the total profit stayed the same).
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5 Generalization for Profit Functions

This section considers the generality of our results by deriving conditions for general (stage 2) profit functions under which the incentive effects driving our results hold.

First, the cost of innovation, $c_{i|p} \in \mathbb{R}^+$ can be divided into two parts: (1) the sat-

$$A \frac{\frac{C_{GE}}{C_m} \frac{C_{mE}}{C_f} n \frac{C_{GE}}{C_f}}{\frac{C_{GE}}{C_m} \frac{C_{mE}}{C_f} n \frac{C_{GE}}{C_f}} @ \{ \} > \{ \} \quad (14)$$

If the cost of innovation is decreasing, then overall innovation increases with competition if either the return to innovation increases with competition or if the cost of innovation falls more quickly than the return. In a model such as Singh-Vives (1984), where the return to innovation increases with competition, the cost reducing effect of profit sharing contracts simply amplifies the increasing return to innovation. In a Schumpeterian model where the return to innovation falls with competition (such as the one we consider), the rates of change of the return and the cost must be compared.

The cost decreases more quickly than the return to innovation as f increases if and only if 15 holds at a given j .

$$j \frac{E \{ \} @ C f \quad E \{ \} @ C f \quad \frac{C \{ \} }{C f} \quad \frac{C \{ \} }{C f}}{E \{ \} \quad E \{ \}^2} \quad (15)$$

The extent of the both invest region expands with f if there is an increase in the highest j such that $v|p \quad \epsilon|p \quad E \{ \}$. The highest such j is $j_{v|p}$ defined earlier, and then condition 15 yields condition 16. More stringent than Condition 13, Condition 16 requires that the proportional effect on profit when both invest be less negative than a proportional effect on the laggard, where the laggard effect is less negative than in 13 since it is proportional to the average of the two profits.¹⁸ Intuitively, this condition requires that the cost of inducing innovation not only decreases as in Condition 13 but

$G_1 \cdot + \$ f \cdot \{ \}, \frac{C_G}{C_f} @ 3, \text{ then } C_1 + \{ \} @ C @ + s f \cdot \{ \}, \frac{C_G}{C_m} \frac{C_m}{C_f} \cdot \frac{C_G}{C_f}$. Finally, the price-cost margins cancel.

¹⁸Condition 16 is can be r1(n)16 n75(s)(/TT29.96)8(.))TJ /TTn 167 Tf 75(s)(/TT29.96)8(d)-1(i m (king(d)-1(ih.963

with a high enough rate.¹⁹

$$\frac{C_{E_1} \{ @ C f}{E_1 \{ } \quad A \quad \frac{C_{E_2} \{ @ C f}{E_2 \{ n \quad E_2 \{ @ 2} \quad (16)$$

6 Conclusion

This paper analyzes the effect of greater product market competition on innovation using a model that makes two key assumptions. First, the model assumes that two symmetric firms, both of which can innovate, compete as differentiated Bertrand competitors and face a linear quadratic demand function. With this assumption, a firm's benefit from making a non-drastic innovation declines as product market competition increases. Second, the model assumes that a firm can only incentivize managers to innovate by offering them a fixed share of profits. With this assumption, a firm's cost of investing in a non-drastic innovation declines as product market competition increases. The overall effect of increasing product market competition in this model depends on whether the reduction-in-benefit effect or the reduction-in-cost-of-innovating effect dominates. In our paper, we find that the reduction-in-benefit effect dominates where product market competition is either very low or very high, however, the reduction-in-cost effect dominates for intermediate levels of product market competition. Based on these results and our general analysis, the argument that firms with market power are more innovative is weaker once one accounts for one plausible cost of innovating.

Of course, our finding that firms with substantial market power have a high cost of innovating is premised on the assumption that firms can only incentivize managers by offering them linear profit sharing contracts. Thus, at this point, it is useful to revisit this assumption. As noted earlier, economic theory suggests that a linear profit-sharing

contract may perform well in some circumstances, and empirical work suggests that the incentive contracts between firms and top management often have a significant linear profit-sharing component. On the other hand, if innovation is very important, a monopoly firm would have an incentive to use some other type of contract because it does not want to offer managers a significant share of pre-existing profits to gain a comparatively small incremental profit. However, these other types of incentive contracts are likely to be costly because contracts that target one particular goal can harm a firm by diverting attention from other important goals. Hence, irrespective of the incentive contract a monopoly firm uses, such a firm may find it costlier to induce innovation than would a competitive firm.

Put differently, several treatments of agency problems within firms note that agency problems are eliminated if the manager can own the firm. Compared to a monopoly firm, it is much less expensive for a competitive firm to get a manager part of the way

co(m)17(s330(e)-329)-375(t)8(o8(t)-262(30314(m)17(an6(l)-359)-272(s)8(e)9333815(o)10(m(r)12(t)8(i)6(n)1t)8(o

frictions related to the costliness of incentivizing employees are directly related to the ratio of the incremental profit from an innovation to the total profit—a friction that would be smaller for a smaller firm or an up-and-coming firm.

	Firm 1 Profit	Firm 2 Profit
$L > L'$	$L > L' \frac{2E \cdot f \cdot E \cdot f n \{^2}{E \cdot f \cdot E 2 f^2}$	$L > L' \frac{2E \cdot f \cdot E \cdot f n \{^2}{E \cdot n f E 2 f^2}$
$L > G'$	$L > G' \frac{2E f n \{^2 f f^2 E \cdot f n \{^2}{E \cdot f^2 E e f^2^2}$	$L > G' \frac{2E f \{^2 f f^2 E \cdot f^2}{E \cdot f^2 E e f^2^2}$
$G > L'$	$G > L' \frac{2E f \{^2 f f^2 E \cdot f^2}{E \cdot f^2 E e f^2^2}$	$G > L' \frac{2E f n \{^2 f f^2 E \cdot f n \{^2}{E \cdot f^2 E e f^2^2}$
$G > G'$	$G > G' \frac{2E \cdot f \cdot E \cdot f^2}{E \cdot n f E 2 f^2}$	$G > G' \frac{2E \cdot f \cdot E \cdot f^2}{E \cdot f \cdot E 2 f^2}$

Table 1: Stage 2 Payoffs to Investment Decision

	$e' f$	$e' e_{v p}$	$e' e_{ p}$
$e' f$	$\frac{E \cdot f \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{v p} \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{ p} \cdot E \cdot f n \{^2}{2 E \cdot f}$
$e' e_{v p}$	$\frac{E \cdot e_{v p} \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{v p} \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{v p} \cdot E \cdot f n \{^2}{2 E \cdot f}$
$e' e_{ p}$	$\frac{E \cdot e_{ p} \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{v p} \cdot E \cdot f n \{^2}{2 E \cdot f}$	$\frac{E \cdot e_{ p} \cdot E \cdot f n \{^2}{2 E \cdot f}$

Table 2: Stage 1 Payoffs, Assuming Pure Strategy (Asymmetric) Stage 3 Equilibrium in which Manager 1 Invests.

7 Appendix

Proof. Define: $g' E \cdot f$, $i' E \cdot f n \{$, and $k' E g n \{$.

$v|p$: The expression for $v|p' \frac{2\{E \cdot f^2}{E \cdot f^2 E e f^2} E \cdot 2k f \cdot 2k f^2$ is the product of two factors. The first factor is always positive. The second factor has one root in the range $f' f' \cdot f' \cdot \frac{E \cdot f n \{^2}{2 \cdot 2 f n \{}$, such that if $f' f' \cdot f'$ then $v|p' A f$ and if $f' f' \cdot f'$ then $v|p' ? f$. Since $f' f' \cdot f'$ if $f' f'$ then $v|p' A f$. The expression for $\frac{C \cdot v|p}{C f}$ is the product of two factors. The first factor, $\frac{2x^2}{E e f^2 E \cdot f^2}$, is always negative. The second factor is $E \cdot H f n \cdot 2 k^2 f n \cdot H i f \cdot k f^e \cdot e i f^D n \cdot k f^2 n i f$. This second factor has no roots in the range in the range $f' f' \cdot f'$ and is positive in this range. Therefore $\frac{C \cdot v|p}{C f} ? f$.

$d v|p$: Since $d v|p' A v|p$, it is also therefore always positive. The expression $d v|p$ is continuous at $f' f$ and $f' f$. The difference, $d v|p' E f \cdot d v|p' E f$ is positive being a product of two factors: $\frac{x \cdot 2 f}{e E e f^2 E \cdot f^2} A f$

root in $E \setminus f, f$, such that if $f \neq f \neq f$ then $\frac{C}{C_f} \frac{d_v | p}{A f}$ and if $f \neq f \neq f$ then

and f_x results in further implicitly defined functions, which are similarly signed by the Cylindrical Algebraic Decomposition Algorithm. ■

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